
Common Algebra Mistakes

Example: Function Notation

The Goal

Compute $f(g(4))$ if $f(4) = -4$, $g(4) = -2$ and $f(-2) = -1$.

The Mistake

Find the algebra mistake:

$$f(g(4)) = f(4)g(4) = (-4)(-2) = 8$$

Need a hint? Look carefully at the red part of the algebra:

$$f(g(4)) = f(4)g(4) = (-4)(-2) = 8$$

The Correction

$$f(g(4)) = f(-2) = -1$$

An Explanation

The expression $f(g(4))$ does not indicate the product of two function values. In other words, it is not equal to $f(4)$ times $g(4)$. Instead, $f(g(4))$ means to compute $g(4)$ and plug the result into the function $f(x)$. In this case $g(4) = -2$, so $f(g(4)) = f(-2) = -1$. This is an example of *function composition*.